

# ACOTRIS : Real Time and Model Checking

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# First part : Contour of the Project

- RNTL Project
- Objectives
- Needs
- General Architecture

## 1st part – ACOTRIS Project

- RNTL Project (AAP2000/CFP2000) ; supported by M.R. (Ministry of Research)
- Partners : CS, CEA-List, MBDA France, INRIA-IRISA, SiTiA
- Propose a **Methodology** and a **Systemic Approach** (+ tools support) :
  - Integrating methods for **formal Checking/Validation** & **co-design**
  - Independent of any (life) cycle
  - Adapted to the approaches used by the majority of the industrialists
  - Taking into account, by "simple" means,
    - o "Functional or Structural" & "Logic and temporal" **needs**,
    - o **Architecture** constraints (hardware),
  - Which Allows to rationalize the development phases of **Real Time Embedded Systems**

cea **list****MBDA**  
MISSILE SYSTEMS

INRIA

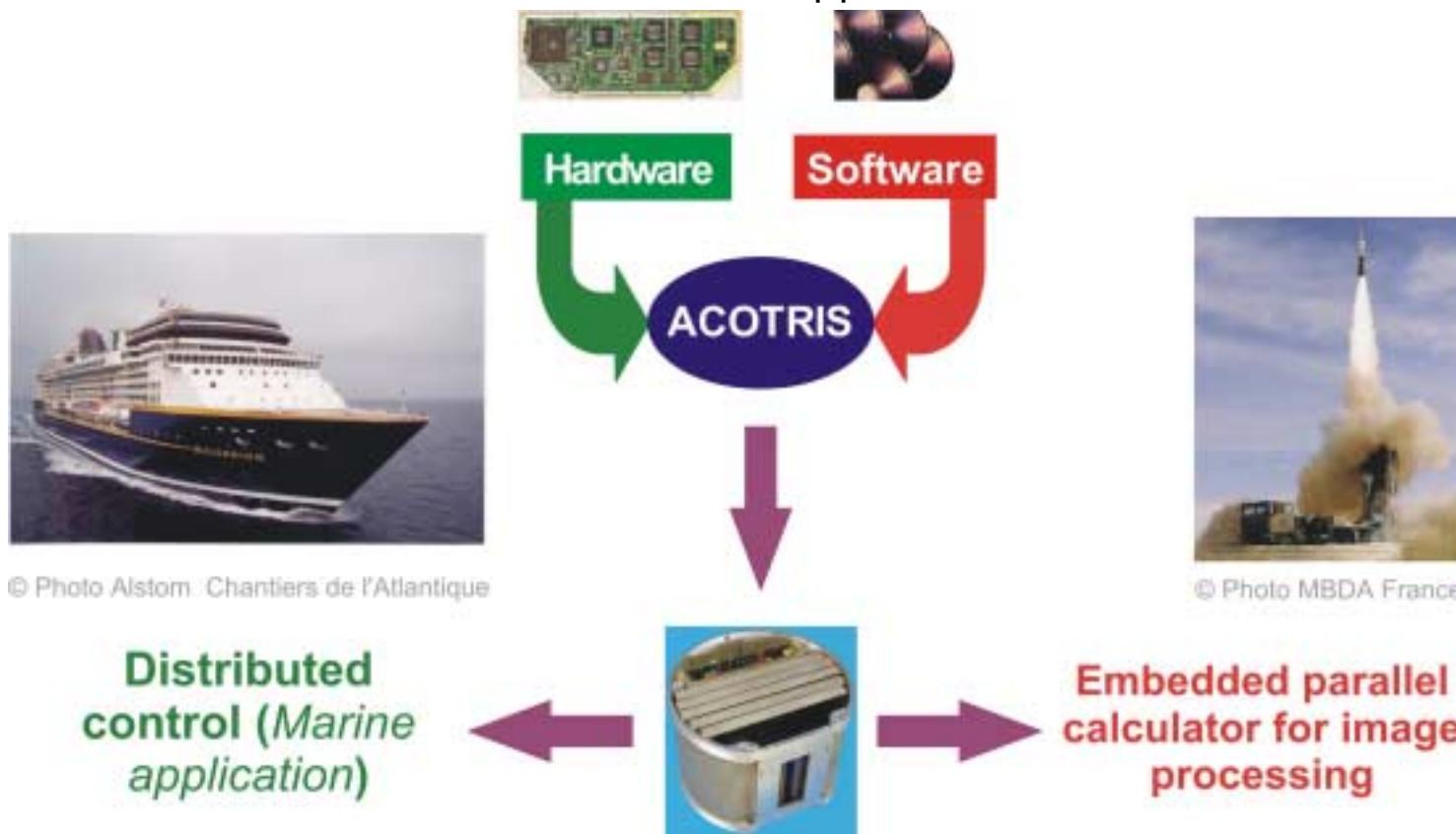
**SiTiA**

## 1st part – Objectives

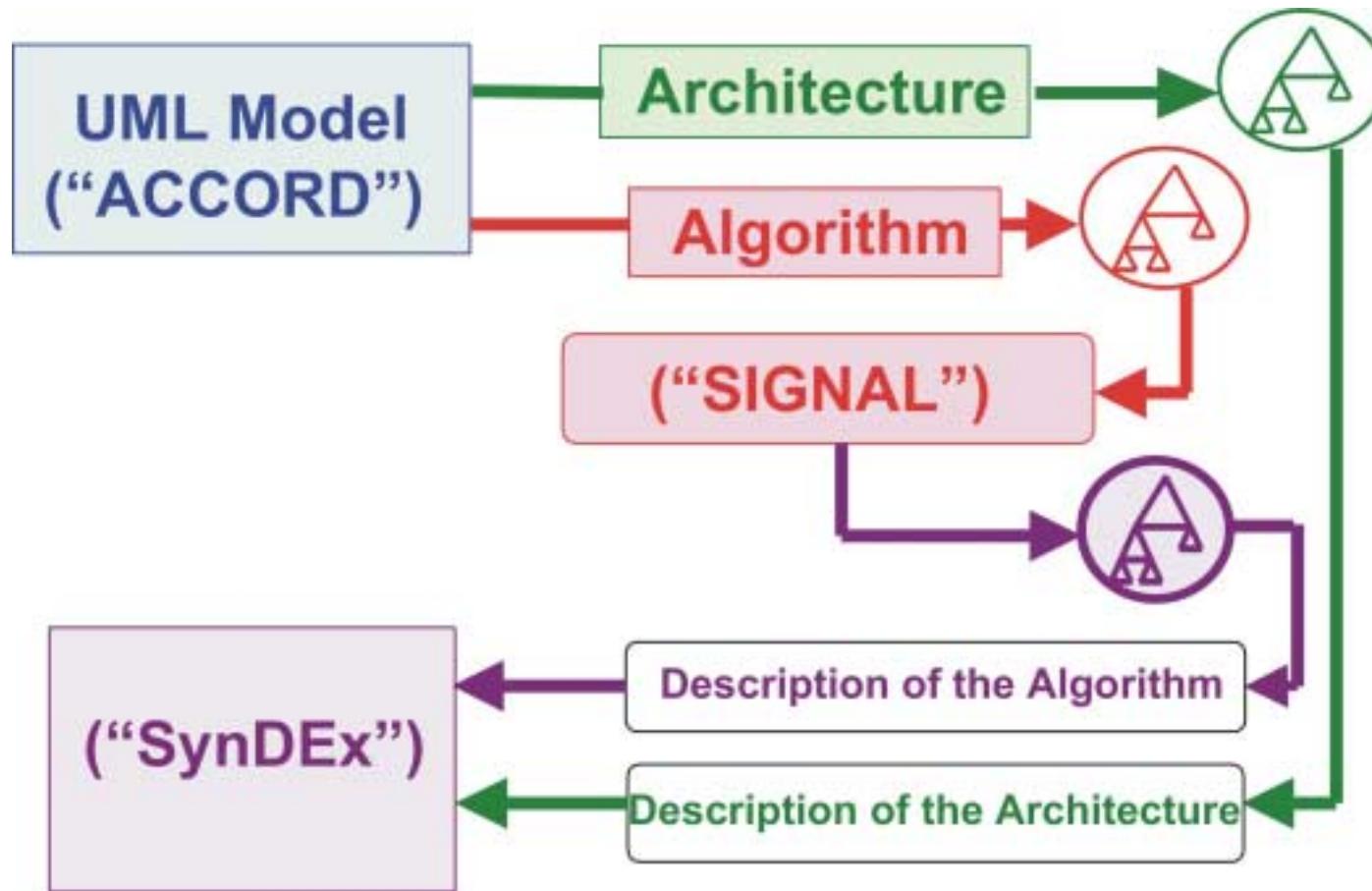
- *To* Help with the complete specification of the need, and the Design of Real Time applications while integrating :
  - An Analysis and Design Methodology based on a standard asynchronous formalism (**UML with ACCORD method ↔ CEA**)
  - A Design and Realization Methodology based on the synchronous model (**SIGNAL and AAA/SynDEX method ↔ INRIA**)
- *In order* To assist the designers of Real Time multi-task applications with strong parallelism during the co-design process by a quasi complete automation of this process
  - **Adapt and connect the existing tools (develop “footbridges”)**

## 1st part - Expression of the need

- Evaluate and validate the technical solutions on two applications :
  - Embedded parallel calculator for image processing
  - Distributed control within a marine application



## 1st part – General Architecture



## 1st part – Anticipated profits

### ● Advantages offered by UML :

- Modularity of the specifications
- Problems separation
- Components re-usability (heritage...)
- Support to the refinement and the legibility of specifications
- Coherent description of various aspects of the system of which :
  - Data Representation
  - Concurrence
  - Expression of the responsibilities in the system

### ● Advantages offered by the synchronous languages :

- Parallelism of the languages (expression) and "centralized code" generation (Compilers)
  - Help to program development :
    - Numerical values
    - Input/output events
    - Optimisation
  - Conformity of the implementation to the specification on the Models level
- ⇒ SAFETY

## Second part

### 1) Boolean Abstraction

- SIGNAL Language
- Boolean Abstraction of a SIGNAL program
- Polynomial Dynamical Systems

### 2) Verification of properties

- Liveness
- Invariance and invariance under control
- Reachability
- Attractivity
- Derived Properties : persistence and recurrence
- Integration in the Polychrony environment for SIGNAL

## 2nd part - The SIGNAL Language

**Environment** for real-time applications

- Synchronous language, data flow oriented

**Signals:**

- Infinite sequences of typed values
- Instants of presence: clock

**Kernel of the language:**

A:=f(B,C)

C:=A default B

(|P1 | P2 |)

B := A\$1 init Bo

C:=A when B

**System of equations**

**Verification and Synthesis of Controllers:** SIGALI

## 2nd part - Boolean Abstraction - General Principle 1

**Signals:** encoded by three values {-1,0,1}:  $F_3$

$$\text{booléens} \Rightarrow \begin{cases} \text{présent} \wedge \text{vrai} \Rightarrow 1 \\ \text{présent} \wedge \text{faux} \Rightarrow -1 \\ \text{absent} \Rightarrow 0 \end{cases} \quad \text{non booléens} \Rightarrow \begin{cases} \text{présent} \Rightarrow 1 \\ \text{absent} \Rightarrow 0 \end{cases}$$

**Operators:**

- Synchronization for non Booleans

$$A := f(B, C) \Rightarrow a^2 = b^2 = c^2$$

- Synchronization and values for Booleans

$$C := A \text{ when } B \Rightarrow c = a(-b - b^2)$$

- The delay (\$): memorization of the previous value in a state variable  $x$

$$B := A\$1 \text{ init } B_0 \Rightarrow \begin{cases} x' = a + (1-a^2)x \\ b = a^2x \\ x_0 = b_0 \end{cases}$$

## 2nd part - Boolean Abstraction - General Principle 2

Signaux booléens	
$B := \text{not } A$	$b = -a$
$C := A \text{ and } B$	$c = ab(ab - a - b - 1)$ $a^2 = b^2$
$C := A \text{ or } B$	$c = ab(1 - a - b - ab)$ $a^2 = b^2$
$C := A \text{ default } B$	$c = a + (1 - a^2)b$
$C := A \text{ when } B$	$c = a(-b - b^2)$
$B := A \$1 (\text{init } b_0)$	$x' = a + (1 - a^2)x$ $b = a^2x$ $x_0 = b_0$
Signaux non booléens	
$B := f(A_1, \dots, A_n)$	$b^2 = a_1^2 = \dots = a_n^2$
$C := A \text{ default } B$	$c^2 = a^2 + b^2 - a^2b^2$
$C := A \text{ when } B$	$c^2 = a^2(-b - b^2)$
$B := A \$1 (\text{init } b_0)$	$b^2 = a^2$

Composition of elementary processes



System of polynomial equations in  $F_3$

$$S = \begin{cases} X' = P(X, Y) \\ Q(X, Y) = 0 \\ Q_0(X) = 0 \end{cases}$$

## 2nd part - Boolean Abstraction - General Principle example

```
process Altern = {? event A,B; !}
( | C := not ZC
| ZC := C$1
| A ^= when C
| B ^= when ZC
)
where boolean C, ZC init false;
```

- Evolution system

$$x' = c + (1 - c^2)x$$

- System of constraints (synchronization)

$$c = -zc, \quad a^2 = -c - c^2, \quad b^2 = -zc - zc^2$$

$$zc = xc^2$$

- System of initialisation

$$x = -1$$

## 2nd part – Polynomial Dynamical Systems

$$S = \begin{cases} X' = P(X, Y) & \text{Evolution equations (functions)} \\ Q(X, Y) = 0 & \text{Constraint equations (invariant)} \\ Q_0(X) = 0 & \text{Initialisation equations} \end{cases}$$

$$X \in F_3^n$$

**State variables**

$$Y \in F_3^m$$

**Event variables**

$$P : (Pi)_{i \in [1..n]} : F_3^{n+m} \rightarrow F_3^n$$

$$Q : (Qi)_{i \in [1..m]} : F_3^{n+m} \rightarrow F_3$$

$$Q_0 : (Q_{0_i})_{i \in [1..n]} : F_3^n \rightarrow F_3$$

## 2nd part - Pol. Dyn. Sys. - Study of the static part

$$\left\{ \begin{array}{l} Q(X,Y)=0 \\ \end{array} \right. \quad \text{Constraint equations (invariant)}$$

**SIGNAL Clock Calculus**

- Solves synchronization constraints
- Structures the control of the application
- Returns a clock hierarchy (forest)

## 2nd part - Pol. Dyn. Sys. - Study of the dynamical part

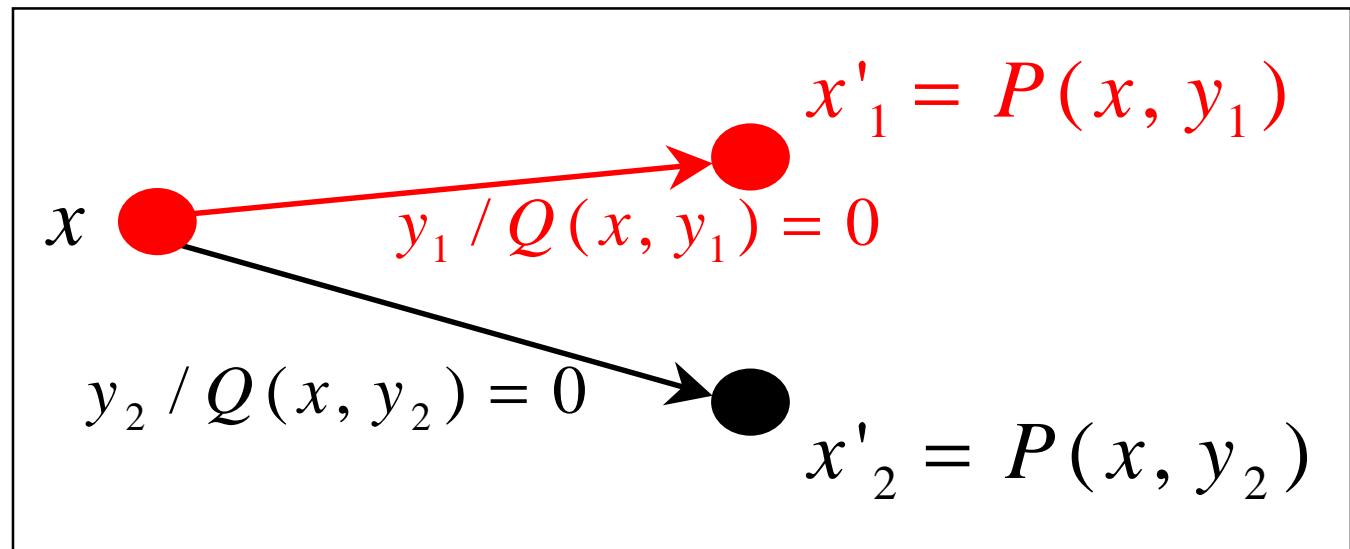
### SIGALI Formal System

- Equation properties equivalent to the properties expressed on sets of states and events
- Systems of equations represented by ideals of polynomials

## 2nd part - Pol. Dyn. Sys. - Underlying explicit automaton

**Initial states:**

$$\{x \in F_3^n / Q_0(x) = 0\}$$

**Evolution:**

## 2nd part - Verification of properties - Liveness

### Definition

- A state  $x$  is alive iff there exists an event  $y$  admissible in  $x$ .
- A set of states is alive iff every state is alive.
- A dynamical system is alive iff, for every state  $x$ , and for every event  $y$  s.t.  $Q(x,y)=0$ , the state  $x'=P(x,y)$  is alive.

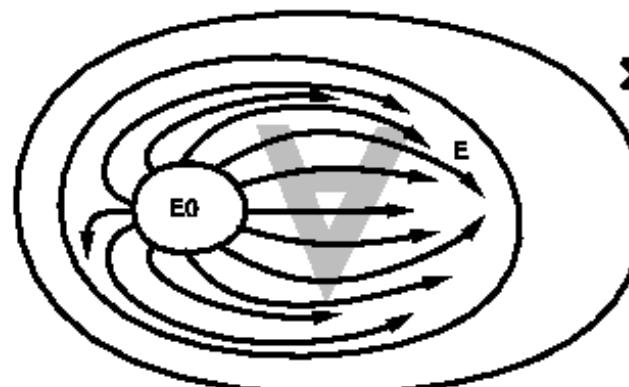
## 2nd part - Verification of properties - Invariance

### Definition

A set of states  $E$  is invariant for a dynamical system, if and only if, for every state  $x$  of  $E$ , and for every event  $y$  admissible in  $x$ , the state  $x' = P(x, y)$  is in  $E$ .

### Set interpretation

$$\forall x \in E, \forall y \in F_3^m, Q(x, y) = 0 \Rightarrow x' = P(x, y) \in E$$



Invariance of  $E$  (from  $E_0$ )

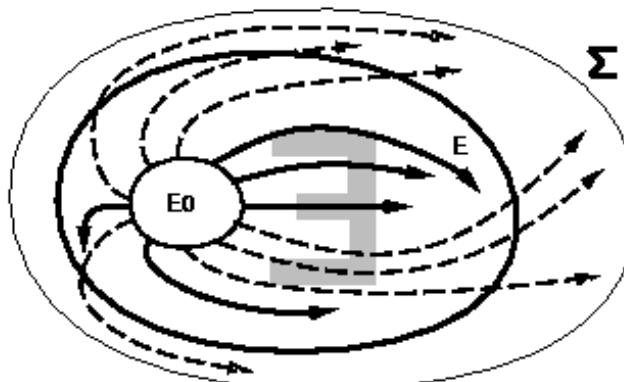
## 2nd part - Verif. of Prop. - Invariance under control

### Definition

A set of states  $E$  is control-invariant for a dynamical system, if and only if, for every state  $x$  of  $E$ , there exists an event  $y$  admissible in  $x$ , such that the state  $x' = P(x, y)$  is in  $E$ .

### Set interpretation

$$\forall x \in E, \exists y \in F_3^m, Q(x, y) = 0 \text{ et } x' = P(x, y) \in E$$



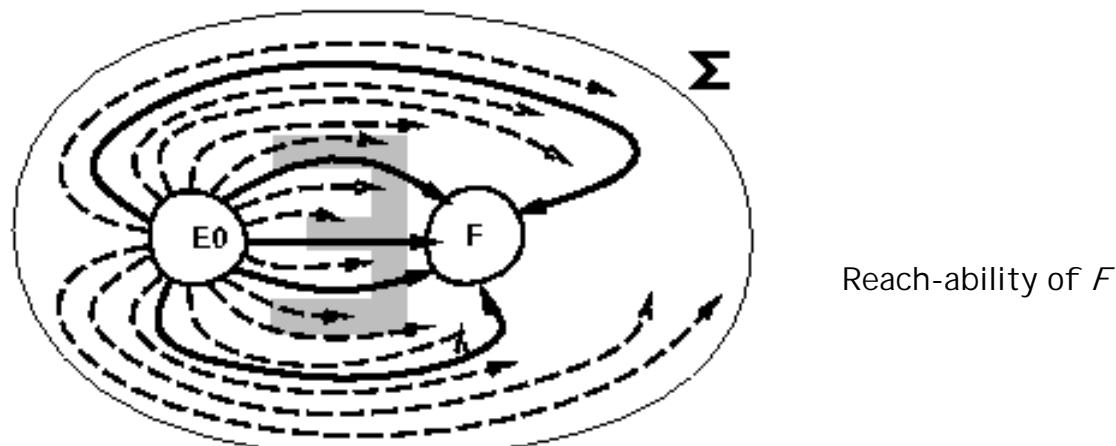
Invariance under control of  $E$  (from  $E_0$ )

## 2nd part - Verification of properties - Reach-ability

### Definition

A set of states  $F$  is reachable for a dynamical system iff every state  $x$  of  $F$  can be reached from the initial states  $E_0$  of the system (i.e., there exists a trajectory initialised in  $E_0$  that reaches  $x$ ).

### Interpretation

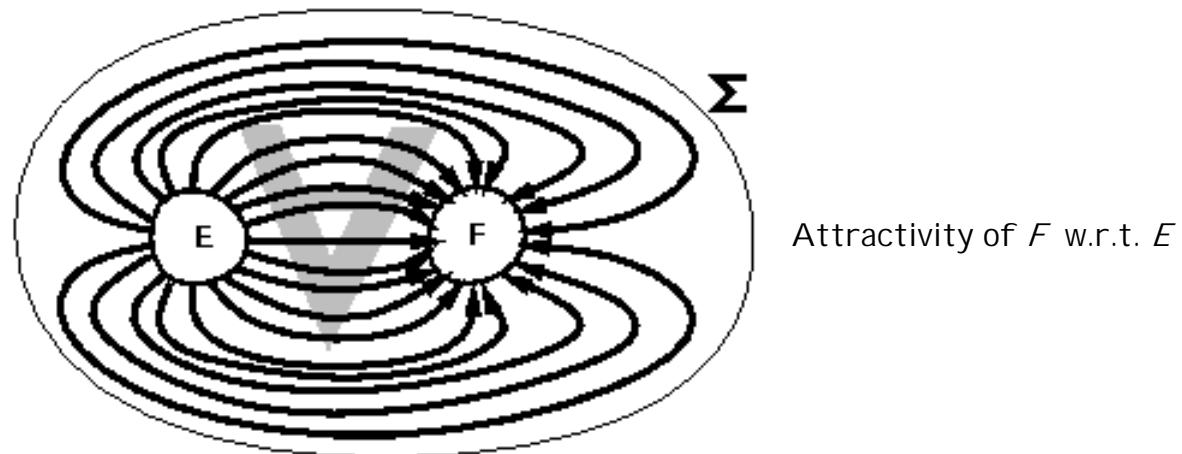


## 2nd part - Verification of properties - Attractivity

### Definition

A set of states  $F$  is attractive for a set of states  $E$  iff every trajectory initialised in  $E$  reaches  $F$ .

### Interpretation



Attractivity of  $F$  w.r.t.  $E$

## 2nd part - Verif. of Prop. - Persistence and recurrence

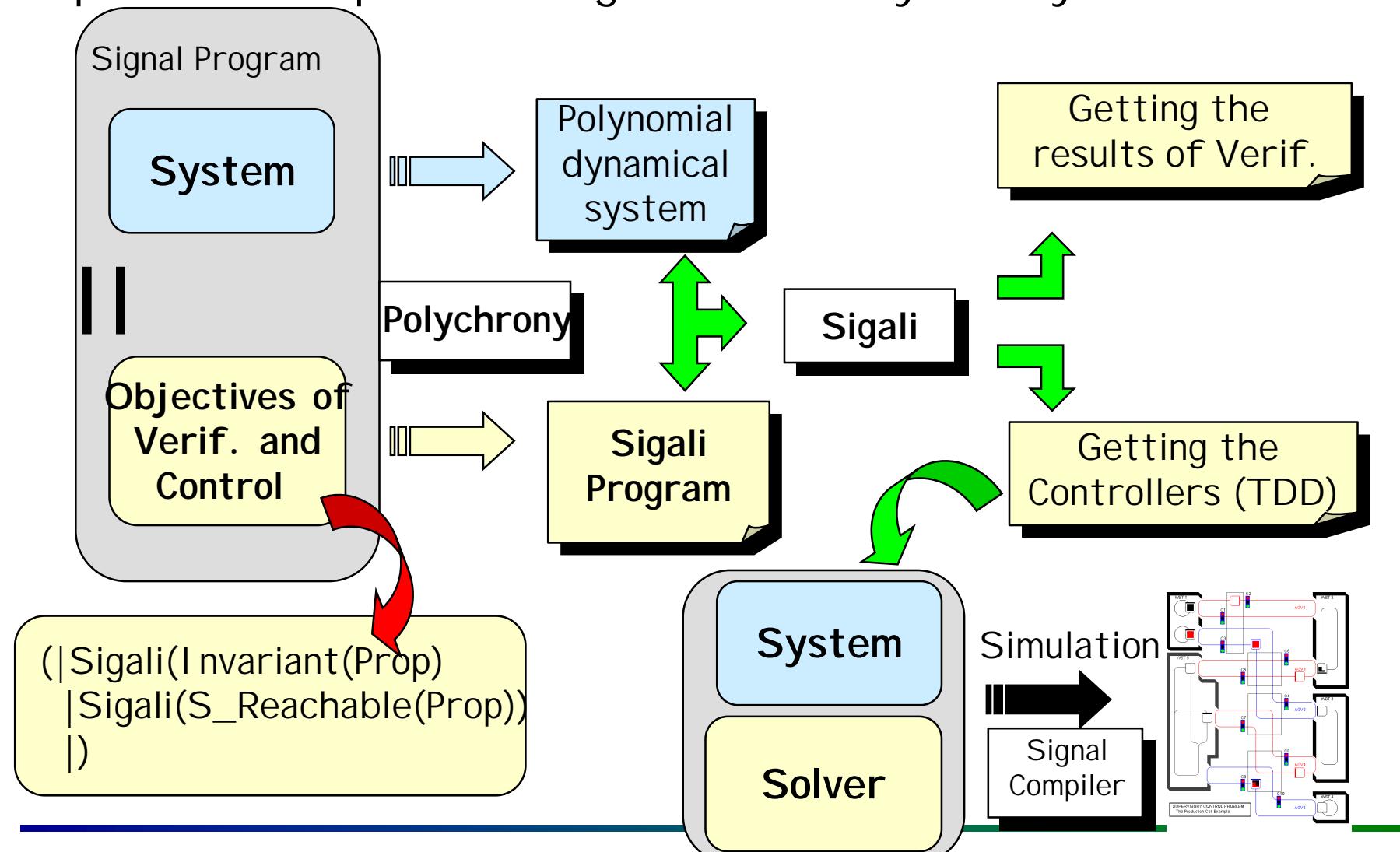
### Persistence

A set of states is persistent iff it is attractive /reachable from the initial states and if it is also invariant.

### Recurrence

A set of states is recurrent iff it is visited infinitely many times.

## 2nd part – Principle of integration in Polychrony / SIGNAL



## 3rd part – The YATUS<sup>(1)</sup> “footbridge”

### 1) ACCORD/UML Methodology

- Overview of the methodology
- The "Drum Regulator" example

### 2) Principles of “UML to Signal” Translation

- Signal language target program structure
- Generation rules

(1) YATUS : Yet Another Translator from UML to SIGNAL

## 3rd part – UML Methodology - Overview

### References and tools

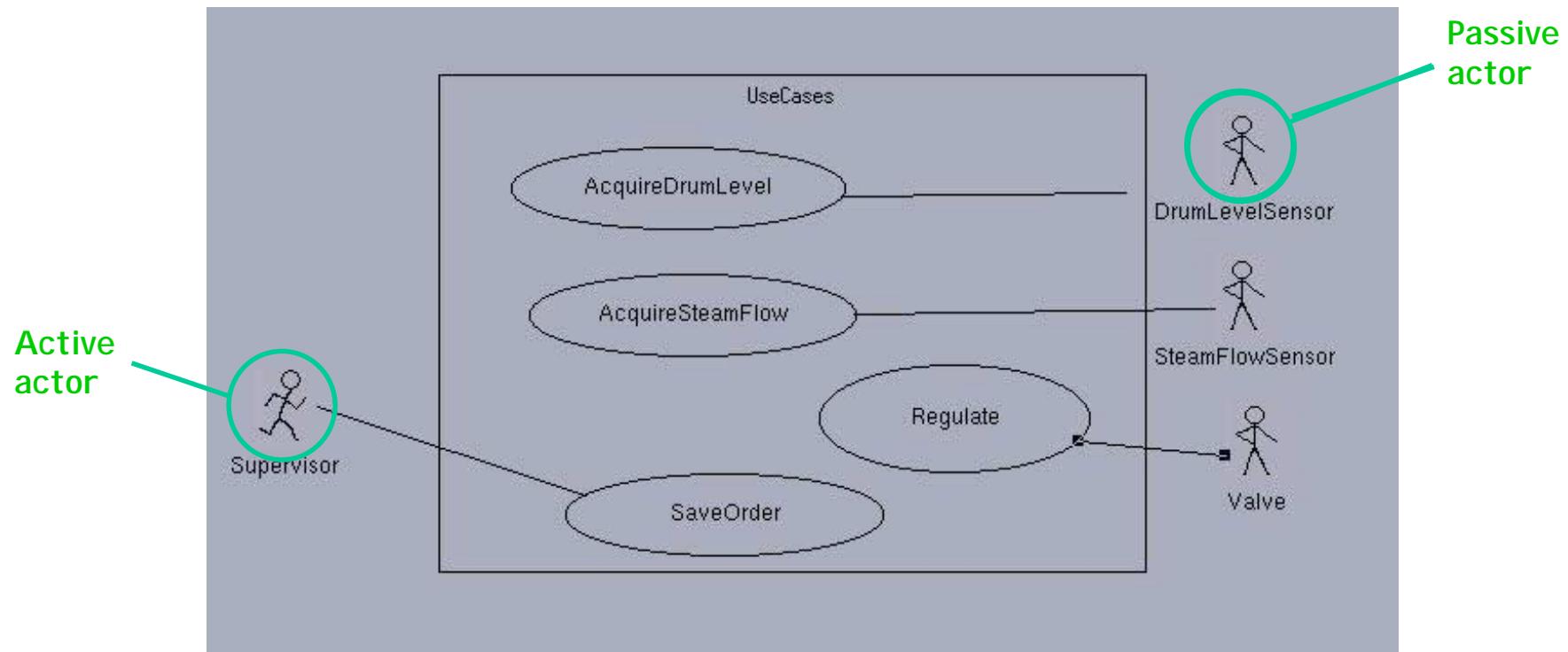
- ACCORD Profile (CEA-LIST)
- Objecteering UML Modeler

### Methodology phases

- Preliminary Analysis Model (PAM)
  - Use cases ([use case diagrams](#))
  - High level scenarios ([sequence diagrams](#))
- Detailed Analysis Model (DAM)
  - Structural view ([class diagrams](#))
  - Behavioural view ([state-transition diagrams](#))
  - Interaction view ([sequence diagrams](#))

## 3rd part - UML Methodology - Overview - PAM

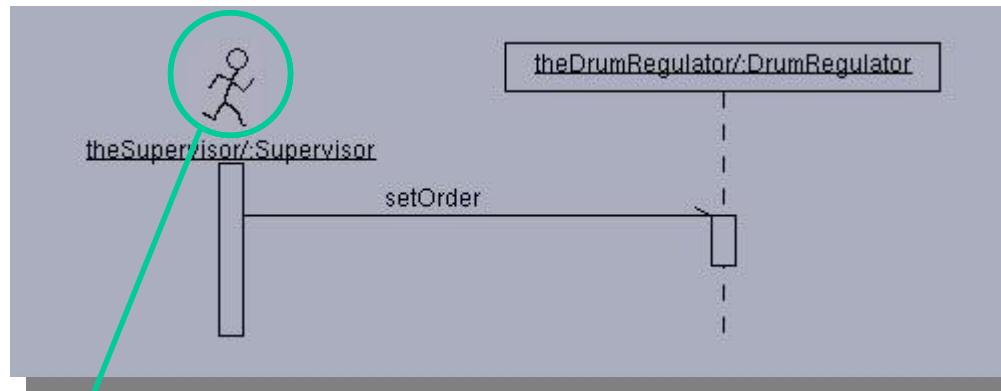
## Use case diagram



## 3rd part - UML Methodology - Overview - PAM

### High level scenario examples

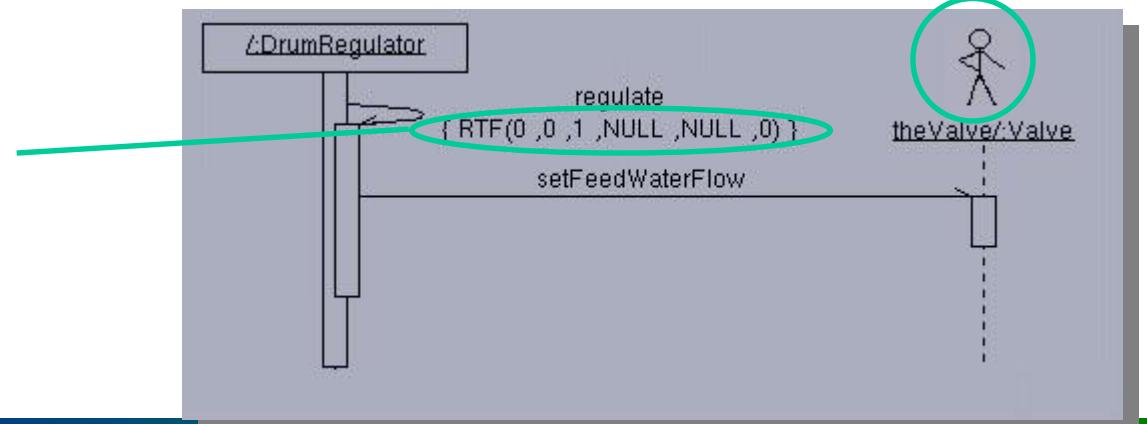
"SaveOrder" scenario



Active actor

Passive actor

"Regulate" scenario



RTF Tagged value for  
real-time constraints

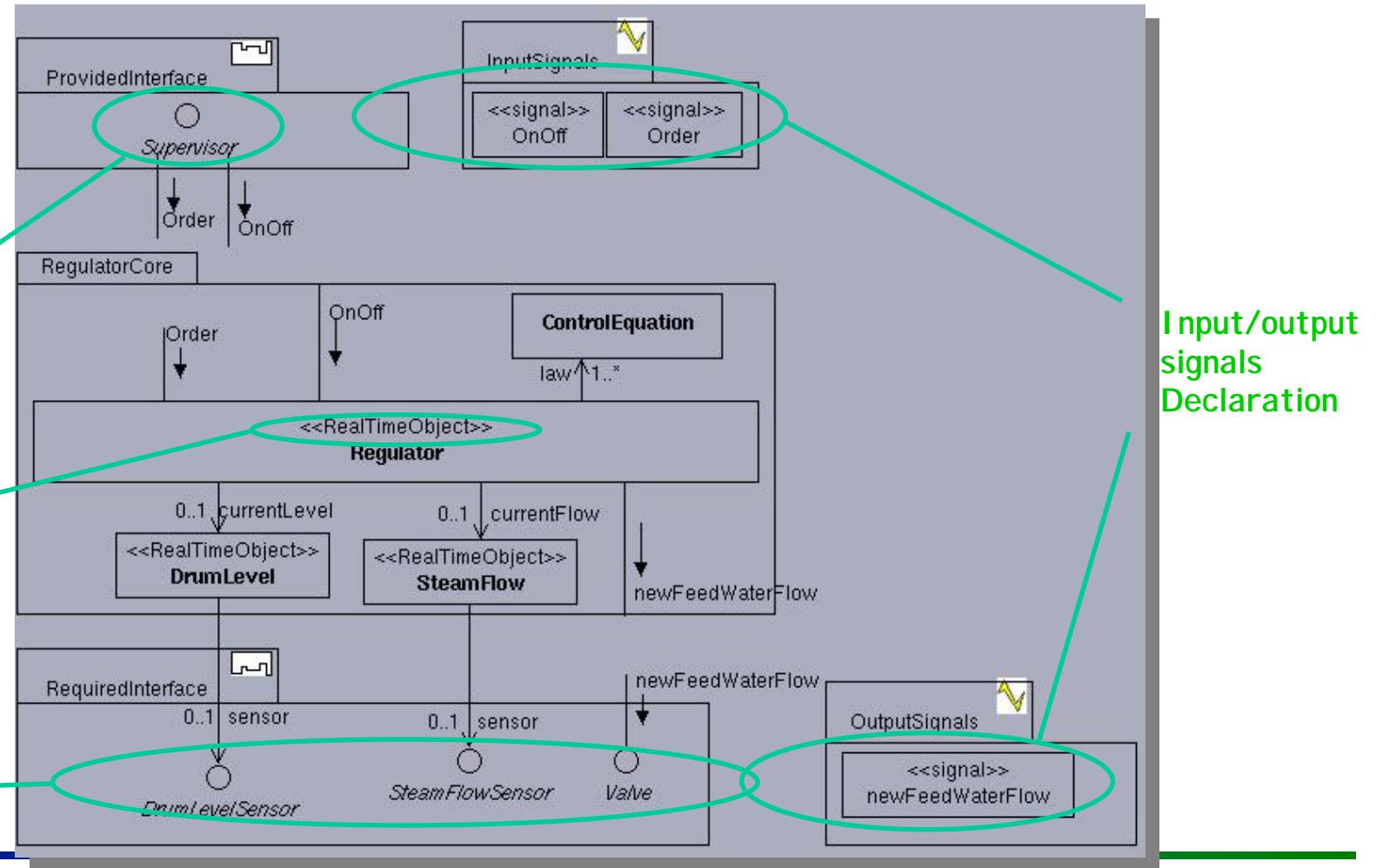
## 3rd part - UML Methodology - Overview - DAM Structural view example

Global class diagram of the system

Transformation of active actors into interfaces

Stereotype for active classes

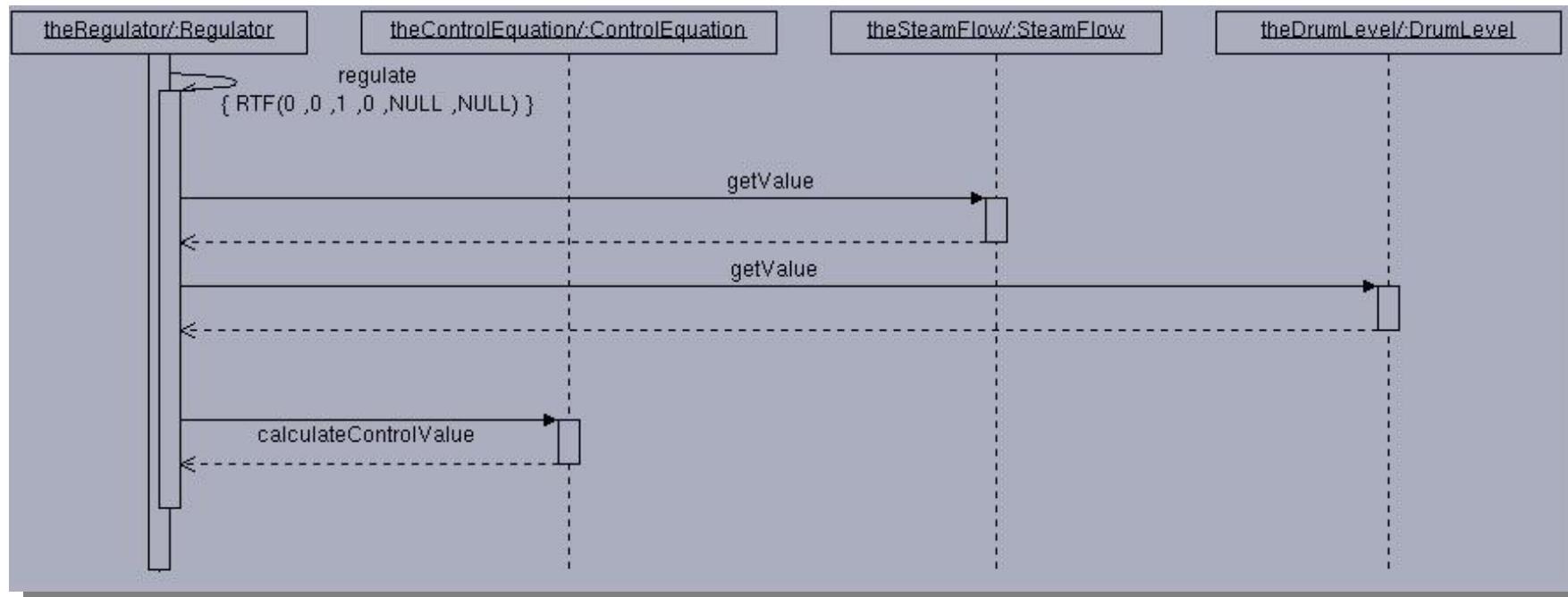
Transformation of passive actors into interfaces



## 3rd part - UML Methodology - Overview - DAM

### Interaction view example

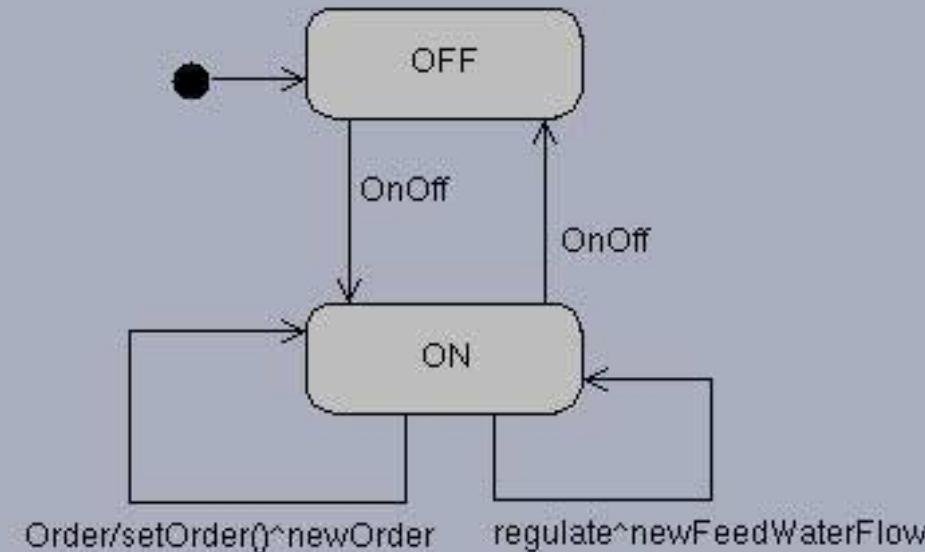
"Regulate" use case detailed scenario



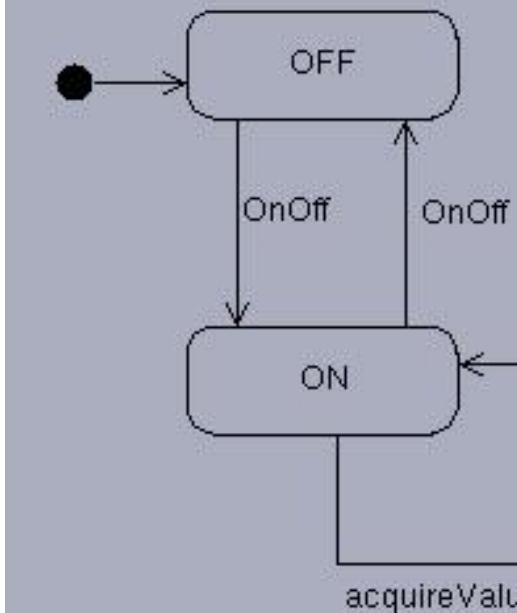
## 3rd part - UML Methodology - Overview - DAM

## Behavioural view example

Regulator Class

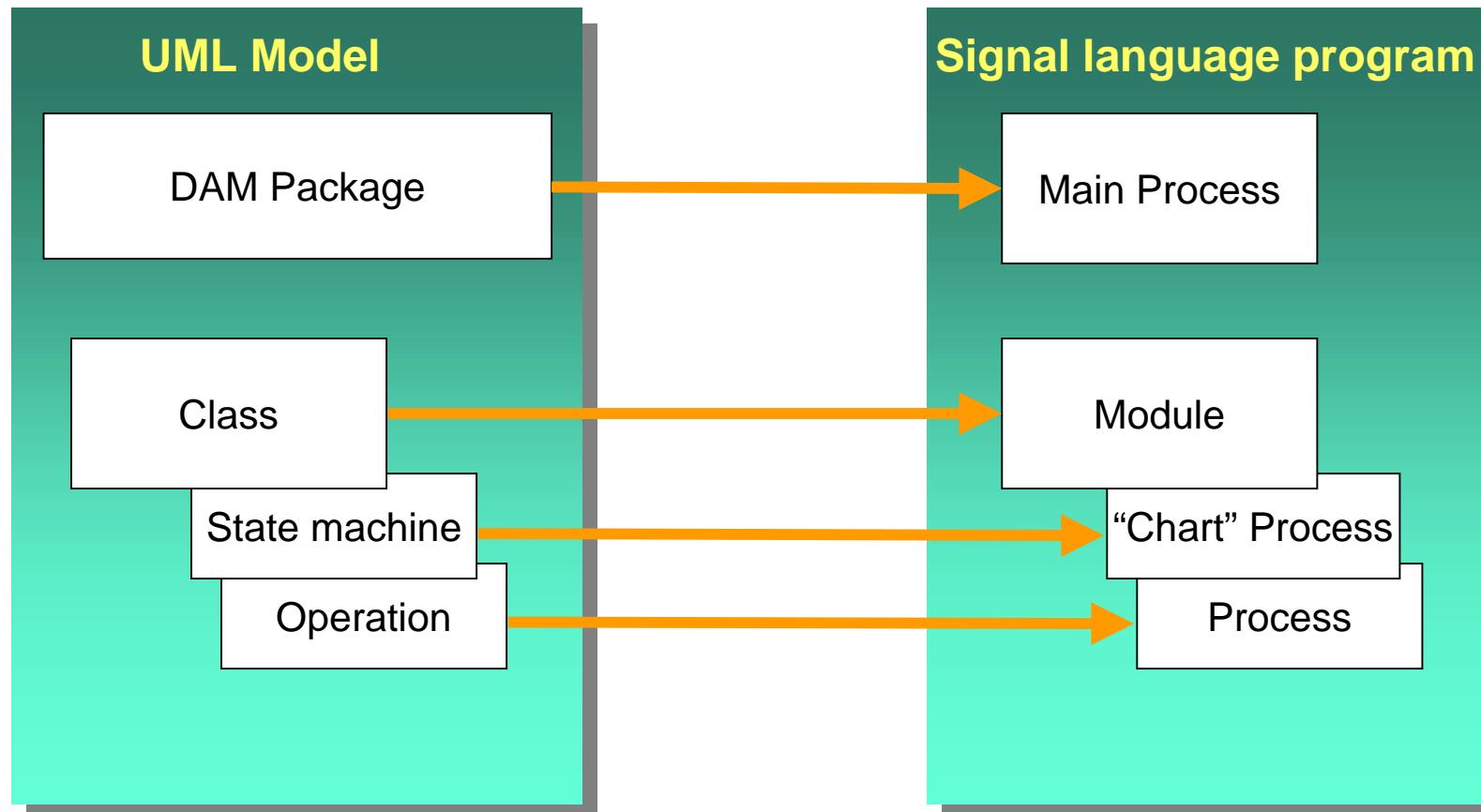


DrumLevel class

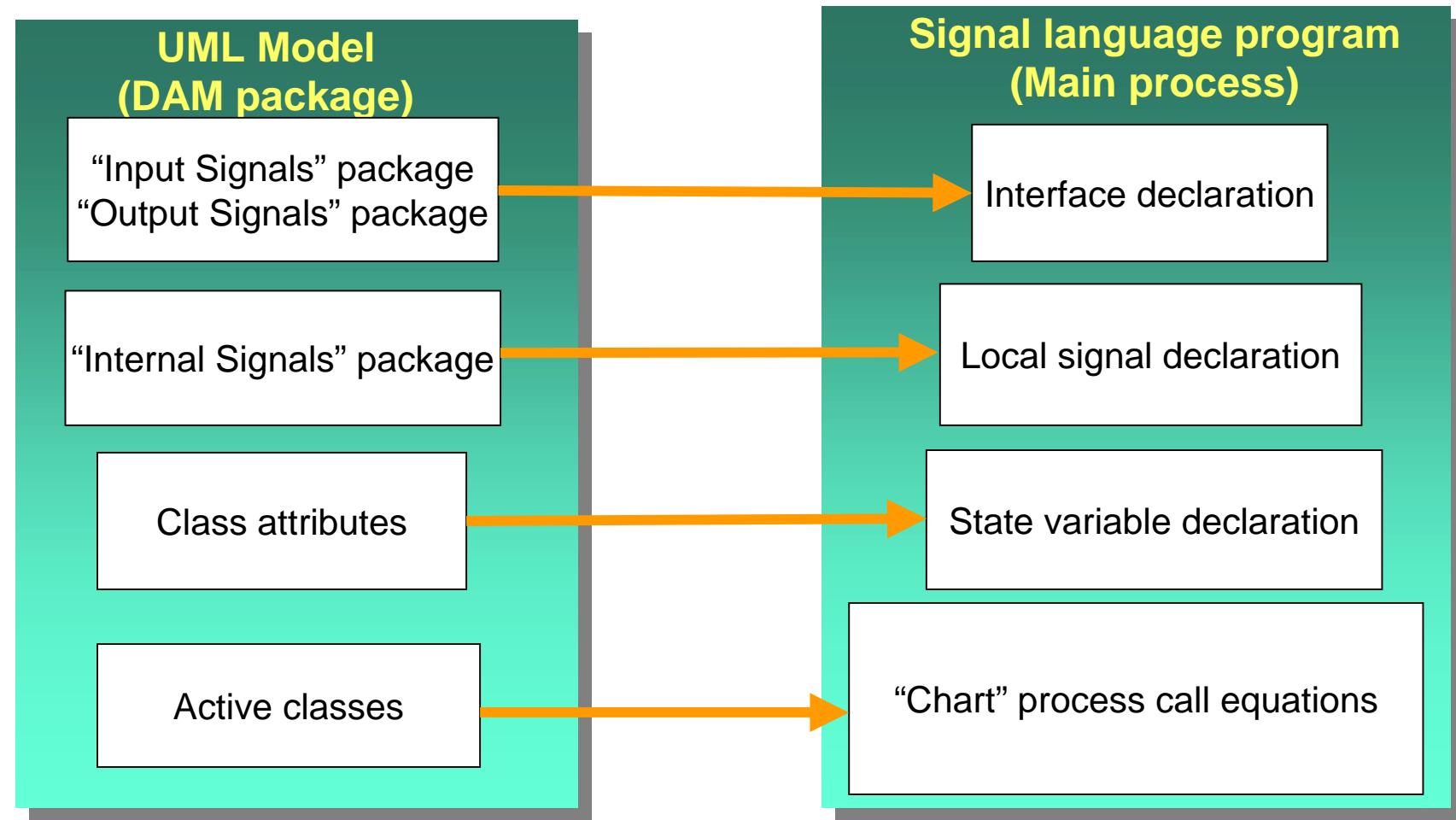


## 3rd part – YATUS Principles

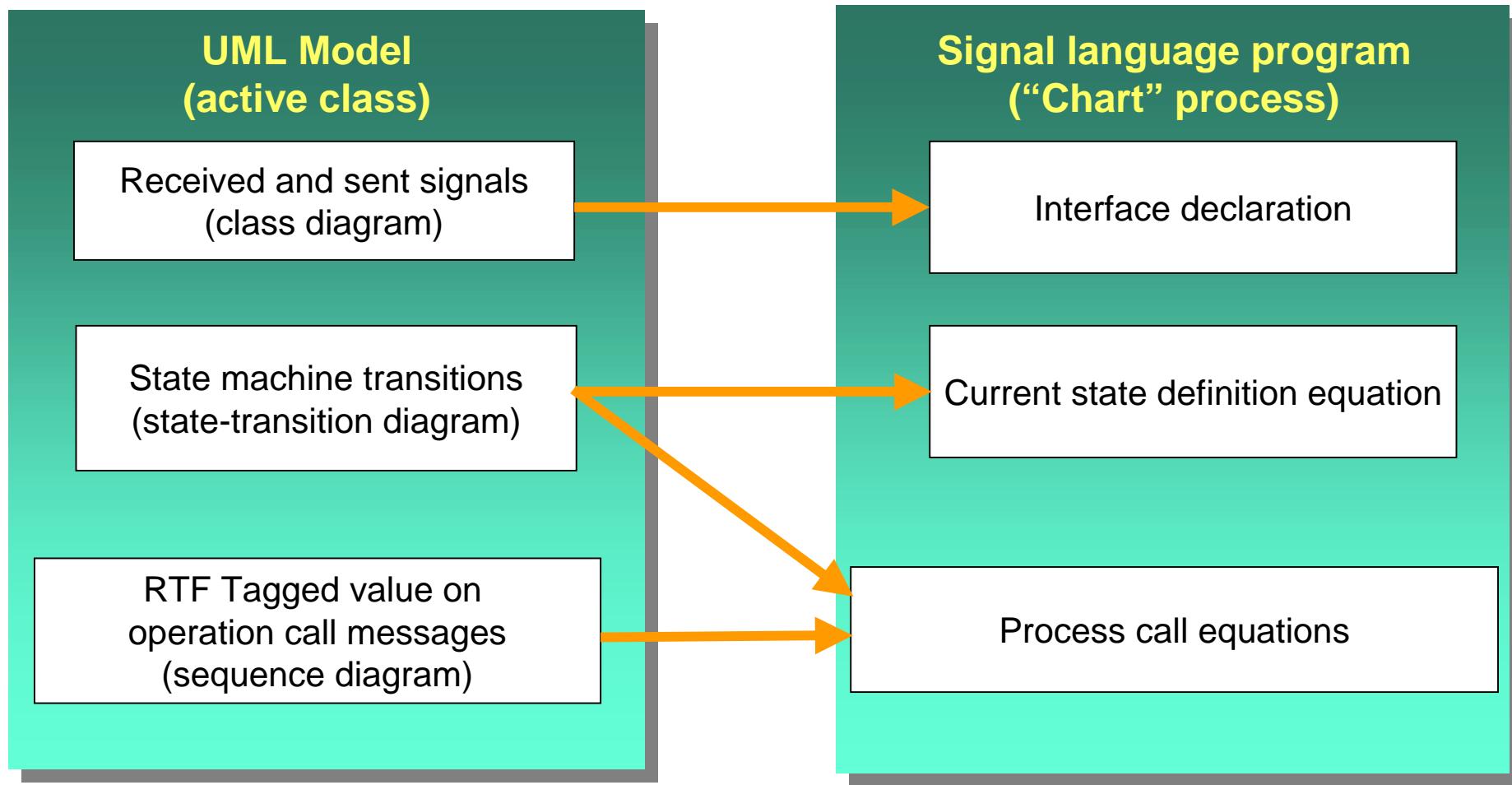
## Signal language target program structure



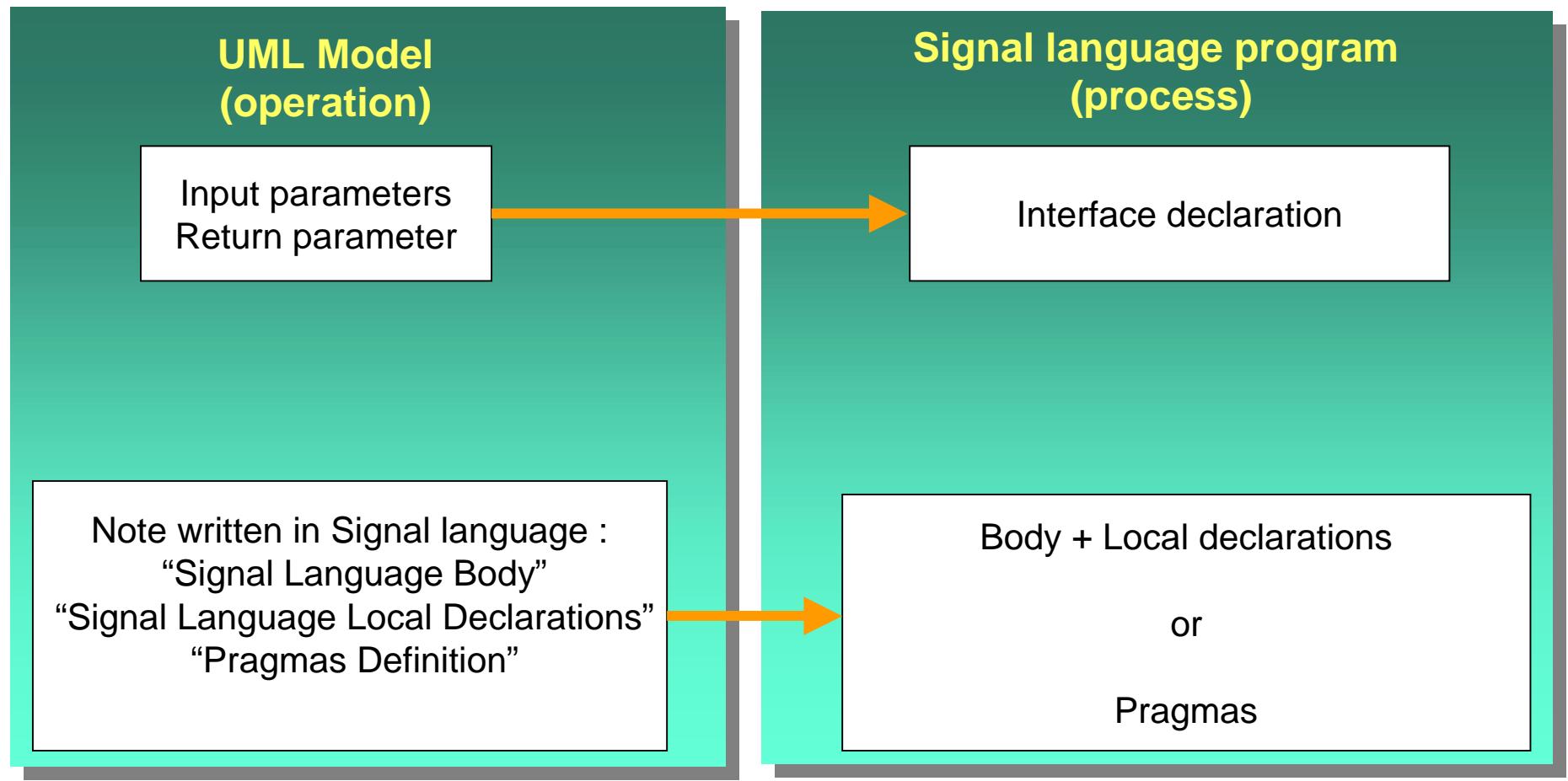
## 3rd part – YATUS : Generation of the “Main” process



## 3rd part - YATUS : Generation of the "Chart" process for an active class



## 3rd part - YATUS : Generation of a process for an operation



## 3rd part - YATUS

# Demonstration